String Techniques for Detecting Duplicates in Document Databases*

Daniel P. Lopresti
dpl@research.bell-labs.com

Bell Laboratories
Lucent Technologies, Inc.
600 Mountain Avenue, Room 2D-447
Murray Hill, NJ 07974

Phone: (908) 582-5428
Fax: (908) 582-3306

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Abstract

Detecting duplicates in document image databases is a problem of growing importance. The task is made difficult by the various degradations suffered by printed documents, and by conflicting notions of what it means to be a "duplicate." To address these issues, this paper introduces a framework for clarifying and formalizing the duplicate detection problem. Four distinct models are presented, each with a corresponding algorithm for its solution adapted from the realm of approximate string matching. The robustness of these techniques is demonstrated through a set of experiments using data derived from real-world noise sources. Also described are several heuristics that have the potential to speed up the computation by several orders of magnitude.

Keywords: *document analysis*, *optical character recognition*, *duplicate detection*, *approximate string matching*, *information retrieval*.

1 Introduction

As information management and networking technologies continue to proliferate, databases of document images and their associated meta-data are growing rapidly in size and importance. A key problem facing such systems is determining whether duplicates already exist in the database when a new document arrives. This is challenging both because of the various ways a document can become degraded and because of the many possible interpretations of what it means to be a "duplicate."

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The U.S. Government's Gulf War Declassification Project, for example, has as its charter the release of documentation that may shed light on the possible causes of Gulf War Illness [9]. To date, over six million pages have been processed, with the ultimate goal of making all of this data available on-line. As can be imagined, the range of documents is enormous, and understanding the ways they relate to one another is a serious problem. In one particular collection activity $564,000$ pages were gathered, the majority of which ($292,000$ pages) were later found to be duplicates of documents already on hand [7]. Hence, the potential for savings in cost and labor is great.

In the case of systems that process incoming documents (*e.g.*, faxes) for later retrieval or for conversion between media types, certain of the steps may be computationally expensive. If it were possible to recognize regions of duplication, some of this extra processing might be avoided by making use of prior results. Moreover, by detecting common content, it may be possible to recognize that one message contains portions quoted (or, perhaps, plagiarized) from another, thereby better understanding their relationship.

Intuitively, the term "duplicate" can be given a number of informal definitions. For example, one document might be a photocopy of another, or a fax. The copies could be visually identical, or one might have additional handwritten notes appended to it. If the original document was generated on-line, a duplicate could contain exactly the same text, only formatted in a different way (changes in font, line spacings and lengths, etc.). A duplicate might possess substantially the same content, but with minor alterations due to editing (*i.e.*, earlier or later versions of the same document). Of course, in any of these cases the scanned image of either or both of the documents may contain significant "noise" due to the way the hardcopy was handled or anomalies in the scanning process. All of these interpretations are reasonable; later a framework is presented for clarifying and formalizing them.

Whatever the definition, the process of determining whether one document is a duplicate of another involves two steps:

1. Extracting appropriate information (features) from the incoming document image.

2. Comparing the features against those previously extracted from documents in the database.

What features to use, and how they are compared, are the two primary issues to be resolved. Different choices lead to models which will be appropriate for different applications.

As to evaluation criteria, speed and robustness are undoubtedly the most important. Speaking in general terms, the more reliable the feature extraction, the better. It should never be assumed, however, that feature extraction is perfect; robustness in the comparison step is crucial. In terms of speed, the second step must be very fast if the database is large and real-time performance is desired. Conversely, requirements for the first step are less stringent if other time-consuming operations need to be performed on the input document anyway. These may include scanning the page in the first place, noise filtering, compression, and in many cases optical character recognition to facilitate later retrieval. In this context, the incremental cost of feature extraction for duplicate detection is likely to be insignificant.

Previous work on detecting duplicates (*e.g.*, [3, 11, 12, 13, 22, 24, 30]) has concentrated mostly on exploring the first step above, turning to more traditional measures when it comes to the second. In several recent papers [16, 17, 18], however, as well as here, the focus is placed on models and algorithms for comparing document representations (*i.e.*, the second step), with features taken to be the uncorrected text output from a commercial OCR package. Presented are a framework for categorizing and studying different kinds of duplicates, as well as algorithms that extend the range of techniques available for searching document image databases. These methods prove to be extremely robust, even in the presence of low OCR accuracies.

The remainder of this paper is organized as follows. Section 2 presents four distinct but related models for the duplicate detection problem motivated in part by the literature for approximate string matching. Each of these is solved optimally using a dynamic programming algorithm, as described in Section 3. Implementation issues are considered in Section 4. In Section 5, several heuristics for speeding up the computation are given. Section 6 presents experimental results that demonstrate the robustness of these techniques across models and in the presence of real-world degradations. Related work is reviewed in Section 7. Finally, conclusions and possible future research directions are discussed in Section 8.

2 Models

For the purposes of this paper, the assumption is that the documents of interest, while in image form, are primarily textual in content. Viewed abstractly, such a page is a series of lines, each consisting of a sequence of symbols. In this *string-of-strings* viewpoint, the term "symbol" can be defined quite liberally. It could be interpreted as meaning characters, of course, but representations at higher levels (*e.g.*, words) or lower levels (*e.g.*, basic features computed from image components) are also possible.

What, then, is a duplicate? Rather than start enumerating possibilities in an ad hoc manner, some structure can be obtained by first partitioning the problem along two dimensions: whether the duplication is full or partial, and whether the layout of text across lines is maintained or not. The reasons for this particular classification scheme are rooted in the string formalisms to be described in the next section. For now, the four possibilities are illustrated with real-world examples and to introduce the terminology:

1. If two documents are visually identical, one is a photocopy or a fax of the other, say, they are *full-layout* duplicates. This category also covers documents distributed electronically (*e.g.*, as PDF or PostScript) and printed without further editing.

2. If two documents have identical textual content, but not necessarily the same layout (*i.e.*, line breaks), they are *full-content* duplicates. This includes, for example, the same e-mail message sent to two people and printed using different-sized fonts, or an HTML document downloaded from the WWW and printed using different margin settings.

3. If two documents share significant content with the same layout, they are *partial-layout* duplicates. Exactly how long the similar regions must be will depend, in general, on the application. Two instances of this are the copy-and-pasting of whole paragraphs from one document into another, and "redacting," the editing of a hardcopy document by obscuring portions of the text so that it is no longer legible.

4. If two documents share content but their layout is not necessarily the same, they are *partial-content* duplicates. This arises in the copy-and-pasting of individual sentences or groups of sentences. A later version of a document that has undergone several editing passes is likely to be a partial-content duplicate.

These various types of duplication are shown in Figure 1. In the next section, algorithms specialized to each of these cases are given. Note that although the text used to illustrate the figure is error-free, it will be necessary to handle a full range of document recognition mistakes, include characters that have been misrecognized, omitted, or added, words that have been improperly segmented, complete lines that have been missed or inserted, etc.

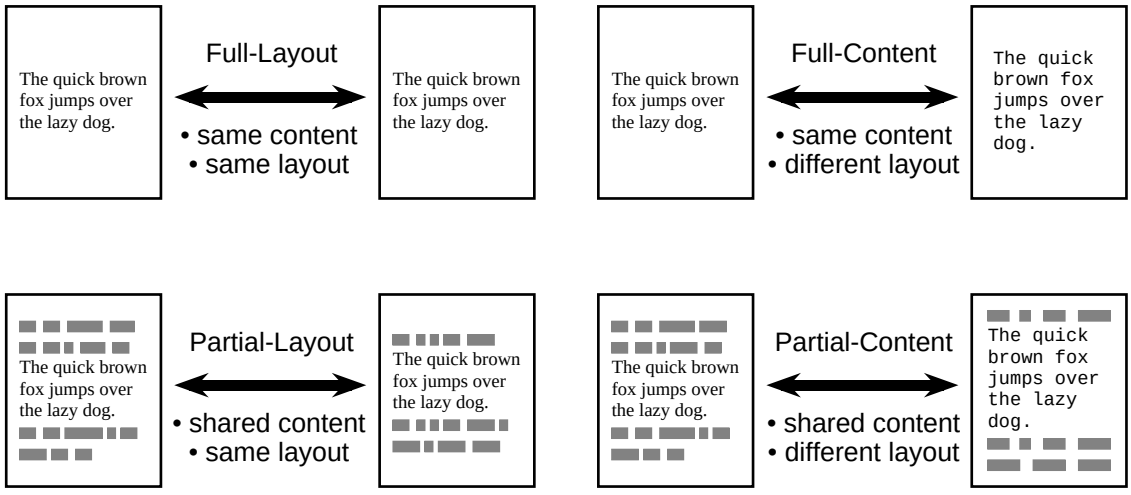

Figure 1: The four duplicate classes introduced in this paper.

Before moving on, it may be instructive to consider briefly the relationships between the various kinds of duplicates. This "universe" is depicted in Figure 2, where several example data-points have also been plotted. Note that there is overlap between the classes, with partial-content duplicates encompassing all the other types.

Clearly, every layout duplicate is also a content duplicate; the former is a special case of the latter. From a formal standpoint, the distinction is whether the page is treated as a 2-D stream consisting of lines made up of characters, or as a 1-D stream of characters in reading order. Note that the 2-D representation can be converted into a 1-D representation by treating the new line character as a space [30]. This implies that any algorithm for detecting content duplicates can also be used to detect layout duplicates. There will undoubtedly be cases, however, where a search can be confined to, say, possible photocopies of a document.

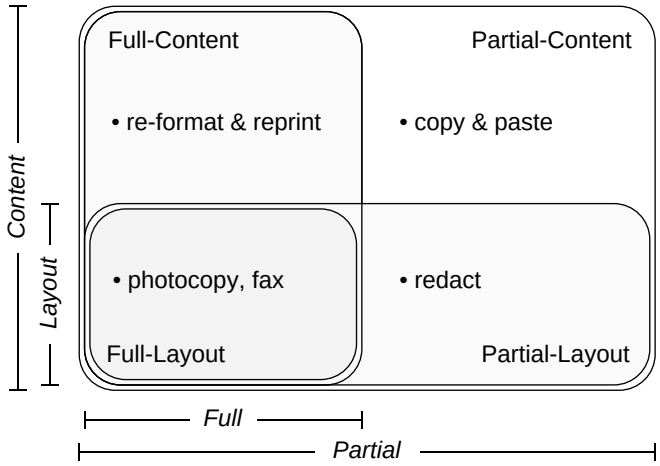

Figure 2: The universe of duplicates.

Here, an algorithm specialized to finding layout duplicates will yield higher precision (*i.e.*, fewer false "hits") than the more general algorithm, which also returns potential content duplicates.

Note also that any full duplicate is also a partial duplicate. Again, there are benefits in maintaining the distinction, both in terms of retrieval precision and because the special case admits heuristics that greatly speed the computation, as will be discussed in Section 5.

3 Basic Algorithms

If it were possible to assume that OCR was perfect or nearly so, the problem of locating duplicates would be relatively straightforward. At best, this is a highly optimistic assumption. Instead, it is safer to acknowledge that OCR can be arbitrarily bad, with no specific guarantee that any n consecutive characters will come through unscathed. If, for example, the accuracy rate were 75% (a reasonable assumption in the case of faxes, small fonts, etc.) and errors are independent, the probability that a given n-gram will survive is 0.24 for $n = 5$, and 0.056 for $n = 10$. The chance that a complete sentence would make it through without errors is slight. Hence, schemes that depend on a majority of words or sentences being recognized correctly, while working reasonably well for clean input, may break down in the case of degraded documents.

Fortunately, the literature on approximate string matching is rich with techniques for addressing such concerns [1, 10, 25, 31]. Moreover, the model correlates well with the physical processes that result in errors, so as a measure of similarity it is supported by intuition. Drawing from this body of work, algorithms are given for each of the four variants of duplicate detection. In the context of their respective models, all are guaranteed to return optimal solutions.

Beginning with some definitions, a *string*, $D = d_1 d_2 \ldots d_n$, is a finite sequence of symbols chosen from a finite alphabet, $d_i \in \Sigma$. String $S = s_1 s_2 \ldots s_m$ is a *substring* of string

$D = d_1 d_2 \ldots d_n$ if $m \leq n$ and there exists an integer k in the range $[0, m-n]$ such that $s_i = d_{i+k}$ for $i = 1, 2, \ldots, m$. The set of all possible substrings of D is denoted D^*. In the 1-D case (*i.e.*, content duplicates), a *document* is simply a string. In the 2-D case (*i.e.*, layout duplicates), a document is a sequence of strings, $D = D^1 D^2 \ldots D^m$ where $D^i = d^i_1 d^i_2 \ldots d^i_n$.

A standard measure for approximate string matching is provided by *edit distance* [14]. In the simplest case, the following three operations are permitted: (1) delete a symbol, (2) insert a symbol, (3) substitute one symbol for another. Each of these is assigned a cost, c_{del}, c_{ins}, and c_{sub}, and the edit distance is defined as the minimum cost of any sequence of basic operations that transforms one string into the other.

3.1 The Full-Content Duplicate Problem

As it relates to full-content duplicates, this optimization problem can be solved using a well-known dynamic programming algorithm [21, 34]. Let $Q = q_1 q_2 \ldots q_m$ be the query document, $D = d_1 d_2 \ldots d_n$ be the database document, and define $dist1_{i,j}$ to be the distance between the first i characters of Q and the first j characters of D. The initial conditions are:

$$\begin{array}{lcll} dist1_{0,0} & = & 0 & \\ dist1_{i,0} & = & dist1_{i-1,0} + c_{del}(q_i) & 1 \leq i \leq m \\ dist1_{0,j} & = & dist1_{0,j-1} + c_{ins}(d_j) & 1 \leq j \leq n \end{array} \tag{1}$$

and the main dynamic programming recurrence is:

$$dist1_{i,j} = \min \left\{ \begin{array}{lcl} dist1_{i-1,j} & + & c_{del}(q_i) \\ dist1_{i,j-1} & + & c_{ins}(d_j) \\ dist1_{i-1,j-1} & + & c_{sub}(q_i, d_j) \end{array} \right. \qquad 1 \leq i \leq m,\ 1 \leq j \leq n \tag{2}$$

The computation builds a matrix of distance values working from the upper left corner ($dist1_{0,0}$) to the lower right ($dist1_{m,n}$), as illustrated in Figure 3. Once it has completed, a sequence of editing decisions that achieves the optimum can be determined via backtracking.

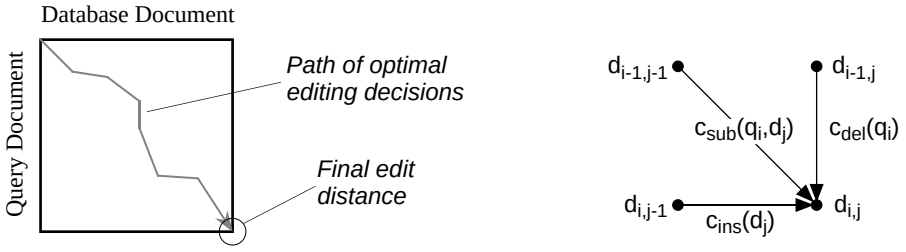

Figure 3: The basic algorithm for string edit distance ($dist1$).

Another way to view the computation is as a shortest path problem for a graph $G = (V, E, w)$, where the vertices correspond to cells in the distance matrix:

$$V = \{(i, j) \mid 0 \leq i \leq m,\ 0 \leq j \leq n\}$$

there is an edge between adjacent vertices related by an editing operation:

$$E = \{[(i-1,j),(i,j)],\ [(i,j-1),(i,j)],\ [(i-1,j-1),(i,j)] \mid 1 \leq i \leq m,\ 1 \leq j \leq n\}$$

and the weights on the edges correspond to the appropriate editing costs:

$$\begin{aligned} w([(i-1,j),(i,j)]) &= c_{del}(q_i) \\ w([(i,j-1),(i,j)]) &= c_{ins}(d_j) \\ w([(i-1,j-1),(i,j)]) &= c_{sub}(q_i,d_j) \end{aligned}$$

All paths from vertex $(0,0)$ to vertex (m,n) correspond to potential sequences of editing operations. The length of the shortest path is the edit distance. This viewpoint, in terms of paths through a graph, will prove useful when heuristics are discussed in Section 5.

As indicated above, the costs in general can be a function of the symbol(s) in question. As a rule, the deletion and insertion costs are assumed to be greater than 0, while the substitution cost is greater than 0 if the symbols do not match and less than or equal to 0 if they do. In the event constant costs are used, it is convenient to refer to them as simply c_{del}, c_{ins}, and c_{sub} (when the two symbols are different) or c_{mat} (when they are the same). It is possible, and indeed sometimes desirable, to specify cost functions that are quite sophisticated. Moreover, the set of basic editing operations can be supplemented as appropriate. Both of these issues will be covered in a later section.

Algorithm *dist1* provides the basis for a solution to the full-content duplicate problem; the smaller the distance, the more similar the two documents. While OCR errors will raise this value somewhat, to the extent they are modeled by symbol deletions, insertions, and substitutions, they will be accounted for.

3.2 The Partial-Content Duplicate Problem

The previous formulation requires the two strings to be aligned in their entirety. For the partial duplicate problem, what is needed is the best match between any two substrings of Q and D. Conceptually, this corresponds to generating all substring pairs in $\{Q^* \times D^*\}$ and then comparing them using algorithm *dist1*. In practice, however, this would be too inefficient.

Fortunately, the original computation can be modified so that shorter regions of similarity can be detected in two longer documents with no increase in time complexity [29]. The edit distance is made 0 along the first row and column of the matrix, so the initial conditions become:

$$\begin{aligned} sdist1_{0,0} &= 0 \\ sdist1_{i,0} &= 0 \quad 1 \leq i \leq m \\ sdist1_{0,j} &= 0 \quad 1 \leq j \leq n \end{aligned} \tag{3}$$

In addition, another term is added to the inner-loop recurrence capping the maximum distance at any cell to be 0. This has the effect of allowing a match to begin at any position

between the two strings. The recurrence is:

$$sdist1_{i,j} = \min \begin{cases} 0 & & \\ sdist1_{i-1,j} & + & c_{del}(q_i) \\ sdist1_{i,j-1} & + & c_{ins}(d_j) \\ sdist1_{i-1,j-1} & + & c_{sub}(q_i, d_j) \end{cases} \qquad 1 \le i \le m,\ 1 \le j \le n \qquad (4)$$

Finally, the resulting distance matrix is searched for its smallest value. This reflects the end-point of the best substring match. The starting point can be found by tracing back the sequence of optimal editing decisions. Note there is an added requirement that the cost when two symbols match be strictly less than zero, otherwise every entry in the matrix will be 0. This computation is illustrated in Figure 4.

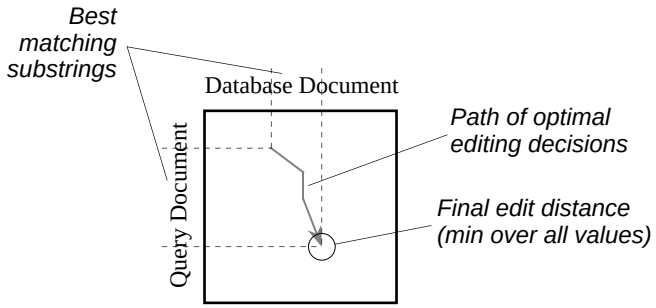

Figure 4: The substring algorithm for edit distance (*sdist1*).

Algorithm *sdist1* solves the partial-content duplicate problem by computing

$$\min\{dist1(A, B) \mid A \in Q^*,\ B \in D^*\}$$

In other words, it locates the best-matching regions of similarity between the two documents Q and D. A and B, the two matching subregions, can be recovered if so desired.

3.3 The Full-Layout Duplicate Problem

For the 2-D models (*i.e.*, layout duplicates), another level is added to the optimization. The problem is still one of editing, but at the higher level the basic entities are now strings (lines). At the lower level, as before, they are symbols. Say that $Q = Q^1Q^2 \ldots Q^k$ and $D = D^1D^2 \ldots D^l$, where each Q^i and D^j is itself a string. For full-layout duplicates, the inner-loop recurrence takes the same general form as the 1-D case:

$$dist2_{i,j} = \min \begin{cases} dist2_{i-1,j} & + & C_{del}(Q^i) \\ dist2_{i,j-1} & + & C_{ins}(D^j) \\ dist2_{i-1,j-1} & + & C_{sub}(Q^i, D^j) \end{cases} \qquad 1 \le i \le k,\ 1 \le j \le l \qquad (5)$$

where C_{del}, C_{ins}, and C_{sub} are the costs of deleting, inserting, and substituting whole lines, respectively. The initial conditions are defined analogously to Equation 1.

Since the basic editing operations now involve full strings, it is natural to define the new costs as:

$$\begin{aligned} C_{del}(Q^i) &\equiv dist1(Q^i, \phi) \quad (= \sum_{k=1}^{|Q^i|} c_{del}(q_k^i)) \\ C_{ins}(D^j) &\equiv dist1(\phi, D^j) \quad (= \sum_{k=1}^{|D^j|} c_{ins}(d_k^j)) \\ C_{sub}(Q^i, D^j) &\equiv dist1(Q^i, D^j) \end{aligned} \tag{6}$$

where ϕ is the null string. Hence, the 2-D computation is defined in terms of the 1-D computation. This is illustrated in Figure 5.

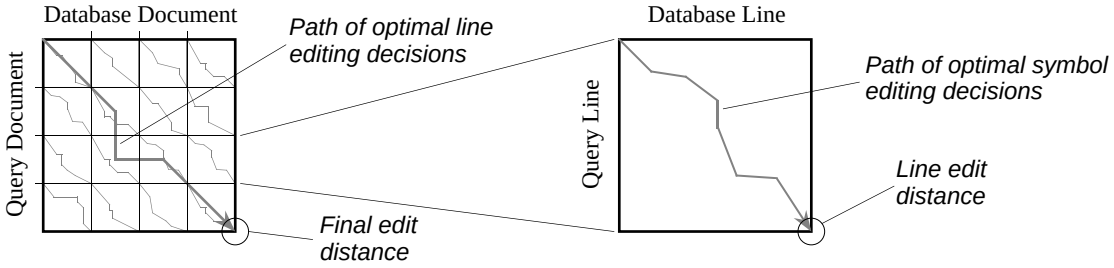

Figure 5: The 2-D algorithm for edit distance (*dist2*).

All else being equal, it can be shown that $dist2(Q, D) \geq dist1(Q, D)$ for any two documents Q and D. As noted earlier, *dist1* admits a larger class of duplicates (full-content), while *dist2* may provide higher precision for the class it is intended for (full-layout).

3.4 The Partial-Layout Duplicate Problem

Lastly, the extension for partial-layout duplicates combines the modifications for the partial (Equation 4) and layout (Equation 5) problems:

$$sdist2_{i,j} = \min \begin{cases} 0 & & & \\ sdist2_{i-1,j} & + & C_{del}(Q^i) & \\ sdist2_{i,j-1} & + & C_{ins}(D^j) & \\ sdist2_{i-1,j-1} & + & C_{sub}(Q^i, D^j) & \end{cases} \qquad 1 \leq i \leq k,\ 1 \leq j \leq l \tag{7}$$

Note that C_{del}, C_{ins}, and C_{sub} are defined as before in terms of *dist1* (*i.e.*, Equation 6), not in terms of the 1-D substring computation as might be expected. The granularity of this matching is whole lines. As before, the resulting matrix must be searched for its smallest value, and then traced back to find where the match starts.

At this point four different algorithms have been presented, one for each of the models described in Section 2.

4 Implementation Issues

In this section, a number of issues associated with implementing the algorithms of the previous section are addressed. The inner loops are straightforward to code, as demonstrated in the case of *dist1* in Figure 6. Even so, there are numerous degrees of freedom and possible extensions that, while they do not change the underlying algorithm, do alter the nature of the computation in interesting and possibly useful ways.

```
for i = 1 to m {
    for j = 1 to n {
        ddel = dist[i-1,j] + cdel(q[i])
        dins = dist[i,j-1] + cins(d[j])
        dsub = dist[i-1,j-1] + csub(q[i], d[j])
        dist[i,j] = MIN(ddel, dins, dsub)
    }
}
```

Figure 6: Pseudo-code for the algorithm *dist1*.

4.1 Input Alphabet

Generally, string algorithms are viewed as operating on character data. While this provides a natural link to the output from OCR, the algorithms are more general than this and can be used on any representation that obeys a 1-D or 2-D string model. The former views a document as a stream of symbols in reading order, where "symbol" could be any of a variety of features that might be computed from the image including characters, shape codes, word lengths, etc. The latter just adds to this a notion of lines, each a sequence of symbols, again in some reading order. The choice of which set of features to use in a given application will depend on the speed and/or robustness with which it can be computed.

4.2 Cost Assignments

The selection of an algorithm determines the editing model. However, within the context of a single algorithm, the choice of cost functions can have a significant impact. While it is fairly common for implementations of Equations 1-4 to employ constant editing costs, the general way in which the algorithms are formulated is much more powerful than this.

To illustrate, consider the question of white-space errors which are common in OCR. By setting $c_{del}(sp) = c_{ins}(sp) = 0$, in effect not charging for such events, unimportant differences between two OCR'ed versions of the same documents can be ignored. Through an appropriate choice of cost functions, the distinction between various input representations is also eliminated. For example, characters and shape codes will yield identical results if the cost of character substitutions is determined based on shape code classes (*e.g.*, $c_{sub}(q_i, d_j) = 0$ for $q_i, d_j \in \{g, p, q, y\}$, the set of descender characters).

If the distribution of the OCR errors can be estimated *a priori* (*e.g.*, via a confusion matrix), this can be exploited by setting the editing costs to be inversely proportional to the frequencies of the error patterns in question. So, for example, if the substitution $e \rightarrow c$ is ten times more likely to occur than $M \rightarrow W$, its cost is made one tenth as much. This will yield a more sensitive comparison; values closer to the minimum when the documents are indeed duplicates under the model in question (differences due to common OCR errors), and further away from the minimum when they are not (true differences).

4.3 New Editing Operations

While the three basic editing operations (deletion, insertion, and substitution) are sufficient to capture all possible differences between two strings, the set can be supplemented with more sophisticated operations to better model an underlying error process. In the case of OCR, it may be desirable to add "split" and "merge" operations to account for mistakes in symbol segmentation [5]. The recurrence for *dist1*, for example, would then become:

$$dist1_{i,j} = \min \begin{cases} dist1_{i-1,j} & + & c_{del}(q_i) \\ dist1_{i,j-1} & + & c_{ins}(d_j) \\ dist1_{i-1,j-1} & + & c_{sub}(q_i, d_j) \\ dist1_{i-1,j-2} & + & c_{split}(q_i, d_{j-1}d_j) \\ dist1_{i-2,j-1} & + & c_{merge}(q_{i-1}q_i, d_j) \end{cases} \qquad 1 \leq i \leq m,\ 1 \leq j \leq n \qquad (8)$$

Other operations such as transpositions can also be supported. In general, as long as the number of symbols involved (the "look-back") is bounded, the recurrence can be augmented without changing the computational complexity of the algorithm.

4.4 Normalization

For exact duplicates, the distance returned by any of the four algorithms of Section 3 will either be 0 or a negative number that grows smaller as the lengths of the documents increase. For dissimilar documents, the maximum distance grows larger as the lengths increase. It is always the case that, for a given query, a smaller distance corresponds to a better match. In order for the results for different queries to be comparable, however, it is necessary to normalize the distances.

If the target interval is $[0, 1]$, where 0 represents a perfect match and 1 a complete mismatch, then the following formula provides an appropriate mapping:

$$normdist = \frac{dist - mindist}{maxdist - mindist} \qquad (9)$$

where *mindist* and *maxdist* are, respectively, the minimum and maximum possible distances for the comparison in question.

Assuming a full-duplicate computation, and making certain reasonable assumptions about the cost functions, the minimum is obtained when all of the characters in the query match the database document and there are no extra, unmatched characters. If the query

is $Q = q_1 q_2 \ldots q_m$, then:

$$mindist = \sum_{i=1}^{m} c_{sub}(q_i, q_i) \tag{10}$$

Or, more simply, $mindist = m \cdot c_{mat}$ when the costs are constant.

The maximum distance, on the other hand, is determined by the query and the set of all strings with the same length as the database document. If the cost functions are unconstrained, this in itself becomes an optimization problem. Fortunately, for constant costs there is a simple closed-form solution. Without loss of generality, let the query be the shorter of the two strings (*i.e.*, $m \leq n$). There are two possible "worst-case" scenarios: either all of the symbols of the query are substituted and the remaining symbols of the database string are inserted, or all of the query symbols are deleted and the entire database string is inserted. Thus:

$$maxdist = \min \begin{cases} m \cdot c_{sub} + (n - m) \cdot c_{ins} \\ m \cdot c_{del} + n \cdot c_{ins} \end{cases} \tag{11}$$

The partial-duplicate computations are normalized similarly.

4.5 Searching Databases

The algorithms given earlier are phrased in terms of quantifying the similarity between strings (documents). The problem of searching a database for duplicates can be cast in two ways:

1. Return the top n matches (in ranked order).
2. Return all documents with distances below a threshold τ.

Note that the first of these requires the computation to complete before any results can be returned to the user. The second can report potential matches as they are encountered (and therefore hide some of the computational latency), but requires setting a threshold in advance. Both policies employ edit distance as a subroutine, and hence can make use of the techniques described to this point.

5 Speeding Things Up

Algorithms *dist1*, *sdist1*, *dist2*, and *sdist2* are optimal in the sense they return min-cost solutions to their respective problems. All require time proportional to the product of the lengths of the two documents being compared. In situations where the resulting database search is too slow, there are a variety of ways to speed things up. These include:

- Computing edit distance faster.
- Avoiding having to compute edit distance for every document in the database.
- Computing an approximation to edit distance.

These approaches can, of course, be used in combination.

Asymptotically faster algorithms (*e.g.*, [2, 33]) and parallel VLSI architectures (*e.g.*, [8, 15]) fall in the first category, while database indexing and hashing techniques (*e.g.*, [4]) occupy the second. Ukkonen, for example, describes an algorithm that could be used to solve the full-content problem that runs in time $O(dist1_{m,n} \cdot \min(m,n))$ provided the cost functions obey certain restrictive assumptions [33]. Bunke presents a preprocessing technique that allows an input document to be compared against a predetermined database in time dependent only on the length of the document [2]. Unfortunately, this requires exponential preprocessing time and, more importantly, exponential space, and hence does not seem practical for large databases. Lipton and Lopresti introduced the notion using a special-purpose, highly parallel VLSI architecture to speed the edit distance computation in cases where the expense of a dedicated hardware solution can be justified [15]. For a more detailed treatment of these and related issues, the reader is directed to the surveys cited in the bibliography [1, 10, 25, 31].

The third category is represented by a well-known heuristic based on the observation that, if two strings are similar, the path of optimal editing decisions must remain near the main diagonal (recall Figure 3). Hence, the computation can be restricted to a band close to the diagonal. Should the edit distance fall below some threshold as determined by the width of the band, the heuristic will return its true value, otherwise it returns a value possibly greater than the true distance (as a path other than the optimal has been chosen). This basic concept, illustrated in Figure 7, has been exploited to speed up the computation in the fields of speech recognition [23] and molecular biology [6].

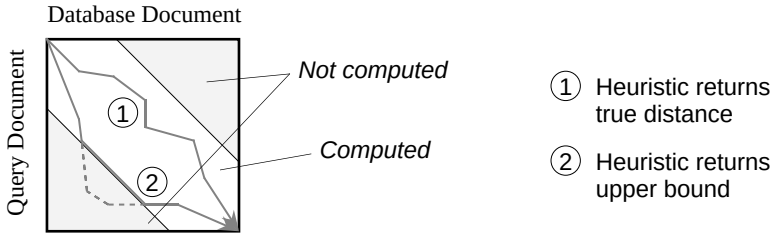

Figure 7: A heuristic for string edit distance.

Note that this heuristic applies only in the case of the full-duplicate versions of the problem, as it assumes the optimal editing path starts at $(0,0)$ and ends at (m,n). In this section, several other techniques are described for speeding up the computation.

5.1 Aborting the Computation

All of the optimal algorithms compute the entire distance matrix even when the strings are not very similar. Likewise, the heuristic just described, although faster, computes the entire length of its band. For certain costs assignments, however, and assuming a threshold τ has been set in advance, it is possible to determine part-way through the computation that no below-threshold solution exists. As a result, the computation can be aborted at this point, with a corresponding savings in time.

Definition 1 *A full-duplicate edit distance computation, dist* $\in \{dist1, dist2\}$*, has the* monotonic increasing property *if the following conditions are satisfied:*

$$c_{del}(q_i),\ c_{ins}(d_j),\ c_{sub}(q_i, d_j) \geq 0 \quad \forall q_i, d_j \in \Sigma \tag{12}$$

Looking at the distance matrix, if the smallest value in a given row is greater than a certain threshold, the final computation can never return a distance less than this. This is because any path from $(0, 0)$ to (m, n), including the optimal one, must pass through this row at some cell, and from that point on the distance will not decrease.

Theorem 1 *Let Q and D be two strings of interest, and* τ *be a predetermined threshold. If a full-duplicate edit distance computation, dist* $\in \{dist1, dist2\}$*, has the monotonic increasing property, and if for some i:*

$$\min_{1 \leq j \leq m} (dist_{i,j}) \geq \tau \tag{13}$$

then $dist(Q, D) \geq \tau$*.*

Hence, if after finishing an iteration of the inner loop (Figure 6) the minimum row distance is found to be greater than the threshold, the remainder of the computation can be skipped; the document in question cannot possibly be a good match. This phenomenon was used by Spitz as a way of deciding when it was safe to abort a comparison [30]. Ukkonen makes an analogous observation [33].

5.2 Pruning the Search

Both of the previous heuristics still fill out portions of the distance matrix in a regular fashion, including cells that have no chance of ever participating in a below-threshold solution. Until all possibility is completely ruled out, the computation must proceed. By taking an even finer-grained approach, however, it is possible to accelerate the process further. Instead of the standard distance matrix, a more flexible data structure is employed: a *livelist* holding cells waiting to be computed that have the potential to be on a path leading to a below-threshold solution.

Let $dist_{i,j}$ be the distance value computed at cell (i, j). By monotonicity, any path to cell (m, n) passing through cell (i, j) must have cost at least $dist_{i,j}$. This is because the continuation of the path can have cost 0, at best.

Lemma 1 *Let Q and D be two strings of interest, and* τ *be a predetermined threshold. If a full-duplicate edit distance computation, dist* $\in \{dist1, dist2\}$*, has the monotonic increasing property, and if* $dist_{i,j} \geq \tau$*, then every path passing through cell* (i, j) *on the way to* (m, n) *has distance at least* τ*.*

In other words, there is no need to continue the computation from cell (i, j) since it cannot possibly result in a solution below the threshold of interest. Note that while Theorem 1 and Lemma 1 both depend on the monotonicity property, the former is a statement about the computation as a whole, whereas the latter is a looser condition that applies to an individual cell.

Lemma 1 gives a criterion for managing the livelist. A given cell is placed on the list if and only if at least one of the cells it depends on is computed and found to be below threshold. Expressed in pseudo-code, the main loop for the 1-D version is given in Figure 8. The computation begins with an initialization phase that places the appropriate cells from the first row and column of the distance matrix on the livelist. The 2-D computation is similar, with the heuristic applied only at the higher level.

```
while livelist not empty {
    remove next (i,j) from livelist

    ddel = dins = dsub = +infinity
    if hdist[i-1.j] was computed then {ddel = hdist[i-1,j] + cdel(q[i])}
    if hdist[i.j-1] was computed then {dins = hdist[i,j-1] + cins(d[j])}
    if hdist[i-1.j-1] was computed then {dsub = hdist[i-1,j-1] + csub(q[i], d[j])}
    hdist[i,j] = MIN(ddel, dins, dsub)

    if hdist[i,j] < threshold then {
        append (i,j+1), (i+1,j), and (i+1,j+1) to end of livelist
    }
}

if hdist[m,n] was computed then {
    return hdist[m,n]
} else {
    return +infinity
}
```

Figure 8: Pseudo-code for the heuristic *hdist1* (compare to Figure 6).

Theorem 2 *Let Q and D be two strings of interest, and τ be a predetermined threshold. If a full-duplicate edit distance computation, dist $\in \{dist1, dist2\}$, has the monotonic increasing property, then the corresponding hdist computation satisfies $hdist(Q, D, \tau) \geq dist(Q, D)$. Furthermore, if $dist(Q, D) < \tau$, then $hdist(Q, D, \tau) = dist(Q, D)$.*

Note that *hdist* is parameterized in terms of the threshold. As will be shown in the next section, it returns all matches below the threshold substantially faster than the corresponding optimal algorithms. Care must be taken when implementing *hdist*, however, as the overhead of replacing a simple data structure (the distance matrix) with the more complex livelist strategy could overwhelm any time savings.

5.3 Pre-Filtering

All of the previous approaches compute edit distance or something that attempts to approximate it in the cases of interest. A different strategy for speeding things up is to look for lower bounds that can be exploited. These are typically fast to compute, and can be used as a pre-filter to decide whether even to begin comparing two strings. For example,

as noted by Spitz [30], if the document lengths are too different there cannot be a match (assuming the cost functions obey certain properties).

A slightly more sensitive version of this is to look for variations in line lengths in the case of full- duplicates. Clearly, a document that has 10 lines of length 100 cannot be a good full-layout match for a document that has 20 lines of length 50, even though their total lengths are identical. At a minimum, the lengths of the lines must be equalized during the editing process, ignoring any possible substitutions that must be accounted for. Note that this measure does not require accessing the document contents, as the line lengths can be stored separately as a compact "handle."

As in solving the full-layout problem, a 2-D string comparison is performed, however the cost functions are defined differently. Let c_{mindel} be the minimum cost for deleting any symbol, $c_{mindel} = \min_{\alpha \in \Sigma} c_{del}(\alpha)$, and c_{minins} be the minimum cost for inserting any symbol, $c_{minins} = \min_{\beta \in \Sigma} c_{ins}(\beta)$. Define *lbnddist2* to be the recurrence specified by Equation 5 when the cost functions are:

$$\begin{aligned} C_{del}(Q^i) &\equiv |Q^i| \cdot c_{mindel} \\ C_{ins}(D^j) &\equiv |D^j| \cdot c_{minins} \\ C_{sub}(Q^i, D^j) &\equiv \begin{cases} 0 & \text{if } |Q^i| = |D^j| \\ (|Q^i| - |D^j|) \cdot c_{mindel} & \text{if } |Q^i| > |D^j| \\ (|D^j| - |Q^i|) \cdot c_{minins} & \text{if } |Q^i| < |D^j| \end{cases} \end{aligned} \tag{14}$$

Note that none of the symbols in the strings need to be examined.

It is easy to show that the individual costs for the *dist2* computation are always at least as large as those for the *lbnddist2* computation:

$$\begin{aligned} dist1(Q^i, \phi) &\geq |Q^i| \cdot c_{mindel} \\ dist1(\phi, D^j) &\geq |D^j| \cdot c_{minins} \\ dist1(Q^i, D^j) &\geq \begin{cases} 0 & \text{if } |Q^i| = |D^j| \\ (|Q^i| - |D^j|) \cdot c_{mindel} & \text{if } |Q^i| > |D^j| \\ (|D^j| - |Q^i|) \cdot c_{minins} & \text{if } |Q^i| < |D^j| \end{cases} \end{aligned}$$

Theorem 3 *Let Q and D be two strings of interest. If a full-layout edit distance computation dist2 has the monotonic increasing property, then the corresponding bnddist2 computation satisfies $dist2(Q, D) \geq lbnddist2(Q, D)$.*

As with *hdist*, *lbnddist2* computes a bound. In this case, however, it is a lower bound, and it is not guaranteed to be tight. By itself, it is not a very good measure of string similarity. It is fast to compute, though, and provides a useful pre-filter for deciding whether to proceed with a given comparison.

It is interesting to note that it may be possible to run *lbnddist2* without performing OCR under certain circumstances. Text lines can be identified and their lengths measured (in terms of pixels) directly from an image. A number of assumptions would need to be made, however, concerning such issues as scaling of the images, the use of different fonts, etc. These topics are beyond the scope of the current paper.

6 Experimental Results

To investigate the performance of the algorithms described in this paper, three sets of experiments were designed. The first examined duplicate detection in the presence of various real-world degradation effects. The second studied the four duplicate models and algorithms and how they relate. Finally, the third experiment sought to quantify the speed-up provided by the heuristics just presented.

The test database consisted of 1,000 professionally written news articles collected from Usenet. The shortest document was 364 characters long, the longest 8,626, and the average 2,974. Hence, the total size of the database was approximately 3 megabytes. This corpus was used as-is (*i.e.*, no attempt was made to inject OCR errors, either real or synthetic). The query documents, however, and the intended duplicates were all "authentic" (pages that had been printed, scanned, and OCR'ed). These documents were formatted in 11-point Times font with a 13-point line spacing using Microsoft Word. Each page was printed on one of two laserprinters, impaired in some way in most cases, scanned at 300 dpi using a UMAX Astra 1200S scanner, and then OCR'ed with Caere OmniPage Limited Edition.

For the full-duplicate computations, the edit costs were set to be $c_{del} = c_{ins} = c_{sub} = 1$ and $c_{mat} = 0$. For the partial-duplicate computations, the match cost was $c_{mat} = -1$. The study of more complex costs assignments (*e.g.*, those based on confusion matrices) is left to a future paper.

6.1 Experiment 1

The goal of this experiment was to study duplicate detection under various noise conditions: copier degradations (multiple generations, excessively light or dark), faxing, and handwritten mark-up (redaction). The source document was 1,395 characters long (26 lines, 203 words). Two sets of six pages were created, one set to be inserted into the database as the intended duplicates, and the other to serve as the queries. The first set was printed on an HP LaserJet 4MPlus laserprinter, the second on an HP LaserJet 4MV. Within each set, one page was used as-is and the others were subjected to one of five different degradations:

Faxed The page was faxed in standard mode from a Xerox Telecopier 7020 fax machine to a Xerox 7042.

3rd Generation The page was copied to the third generation on a Xerox 5034 copier.

Light The page was copied on the same copier with the contrast set to the lightest possible setting.

Dark The page was copied with the contrast set to the darkest possible setting.

Annotated Five separate text lines on the page were completely obscured using a thick blue marker pen. Different lines were excised in the query and database documents. Also, "This is important!" was handwritten in the margin.

The pages were then scanned and OCR'ed. In addition, the original ASCII text for the query document was left in the database. Hence, each of six queries was run against a database

of 1,000 documents containing seven intended duplicates (six that had been OCR'ed, plus the original).

Table 1 below shows the OCR accuracies. Note that the rates range widely, dropping as low as 73.5%. While the two different versions from the same noise source are usually fairly close, they are by no means identical. As expected, a large variety of OCR errors were encountered. Beyond this, other kinds of degradations arose as well. For example, the standard headers prepended to faxes were transcribed (albeit with numerous mistakes), and the lines that had been crossed-out were completely missing from the annotated pages.

	OCR Accuracy	
Document Type	Database	Query
Printed	96.2%	96.0%
Faxed	77.7%	83.9%
3rd Generation	95.9%	96.1%
Light	86.1%	77.8%
Dark	94.0%	95.3%
Annotated	75.6%	73.5%

Table 1: OCR accuracies for test documents from Experiment 1.

Since the query documents and their intended matches have the same layout, this is a full-layout duplicate detection problem and the *dist2* algorithm is most appropriate. The charts in Figures 9-11 plot, for each query, the normalized edit distance for every document in the database. Note that there is always a clear distinction between true duplicates and everything else. This demonstrates that the technique is robust when faced with the sorts of OCR errors seen in practice.

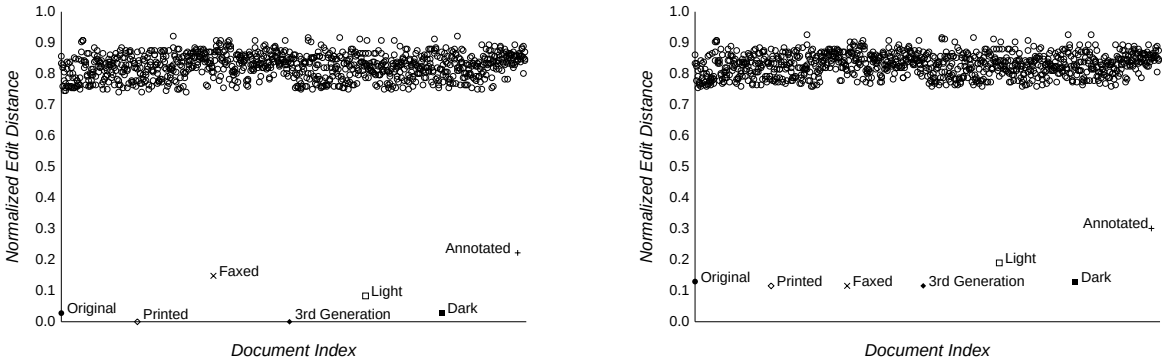

Figure 9: Full-layout duplicate detection for printed (left) and faxed (right) queries.

Studying the data further, it should come as no surprise that the annotated documents yielded the worst-case scenario. Recall that about 20% of the text was completely obscured, a figure that places severe constraints on the performance of any comparison measure. Still, the normalized edit distance in most of the charts is not much greater than this value. When the annotated documents were compared to each other (the right side of Figure 11),

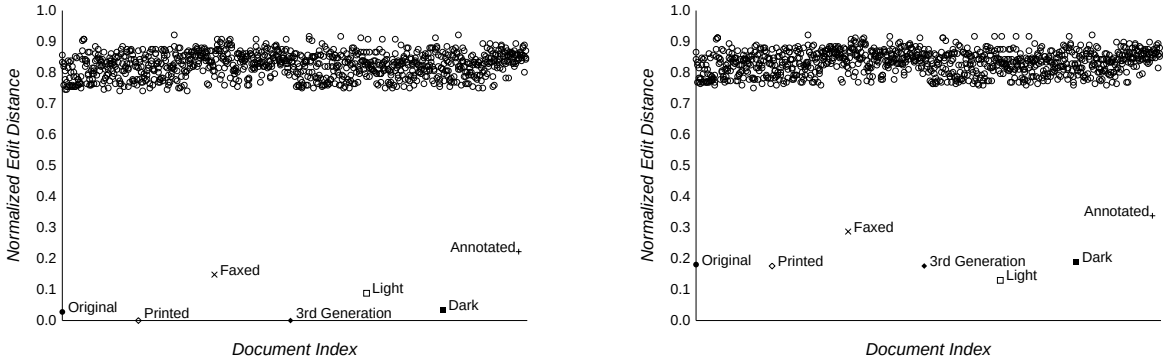

Figure 10: Full-layout duplicate detection for 3rd generation (left) and light (right) queries.

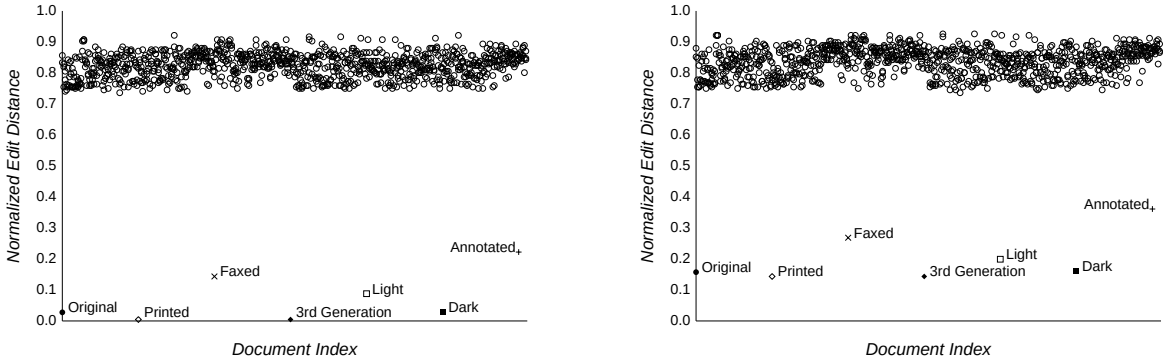

Figure 11: Full-layout duplicate detection for dark (left) and annotated (right) queries.

the amount of text missing between the two amounted to 40%. Even so, and despite all the other OCR errors that must have occurred, it is possible to distinguish the duplicates from non-duplicates.

It is also interesting to note that query and database documents produced using the same noise source are usually a slightly better match (the notable exception being the case of the annotated pages). Whether it is possible to exploit this is a topic for future research.

6.2 Experiment 2

The purpose of this experiment was to determine how the different duplicate models relate empirically. The four algorithms described in Section 3 were run using the same source document as in the previous experiment. Duplicates were constructed from the query by:

1. Changing the line breaks to create a document that was a full-content duplicate but not a full-layout duplicate.

2. Appending roughly equal amounts of unrelated text to the beginning and end of the document to create a partial-layout duplicate approximately twice as long as the original.

3. Combining these first two steps to create a partial-content duplicate.

The pages were then printed, scanned, and OCR'ed. The OCR accuracies appear in Table 2. As before, the original source text was left in the database to serve as a second full-layout duplicate of the query. Hence, there were between two and five duplicates in the database, depending on the model.

	OCR Accuracy	
Document Type	Database	Query
Full-layout	96.0%	95.9%
Full-content	96.1%	n/a
Partial-layout	94.9%	n/a
Partial-content	96.0%	n/a

Table 2: OCR accuracies for test documents from Experiment 2.

The results for this experiment are shown in Figures 12-13. Since there is a fair amount of residual similarity even in the non-matching cases, the normalized edit distances are lower than for purely random documents. Note that, as expected, algorithm *dist2* works best for full-layout duplicates, and *dist1* adds to this full-content duplicates (Figure 12). The partial-layout algorithm *sdist2* can detect full- and partial-layout duplicates, while *sdist1* covers all four duplicate classes (Figure 13).

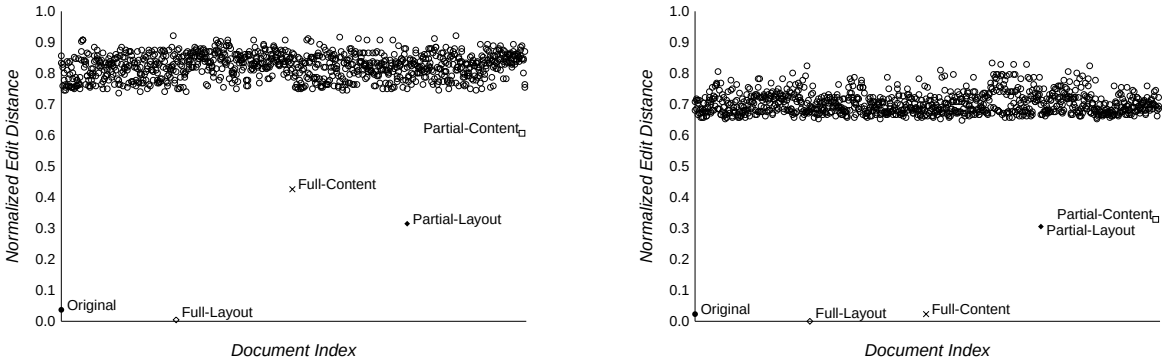

Figure 12: Duplicate detection using algorithms *dist2* (left) and *dist1* (right).

6.3 Experiment 3

The final experiment was designed to study the speed-up potential of some of the techniques described in Section 5. The same database was used as in Experiment 1, with the straight OCR'ed version of the document serving as the query. Hence, there were seven potential duplicates (the six OCR'ed pages and the error-free original).

The algorithms described in this paper were coded in C on an SGI O2 workstation running the IRIX operating system. The O2 was configured with a 200 MHz MIPS R5000

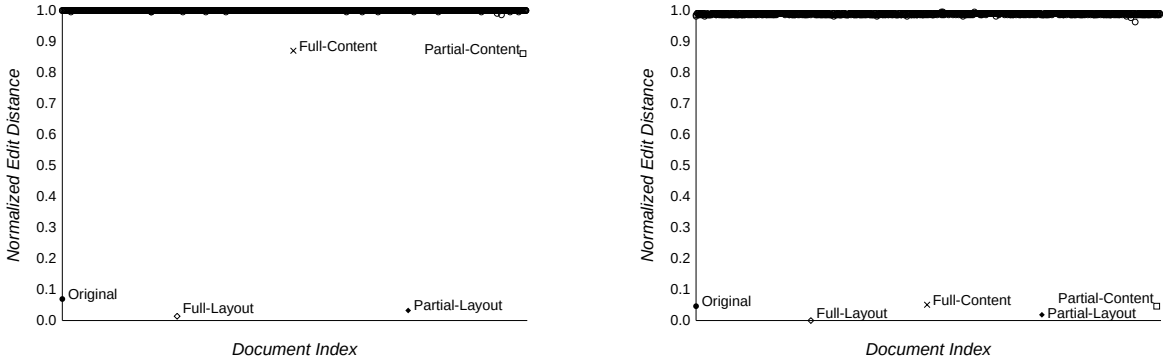

Figure 13: Duplicate detection using algorithms *sdist2* (left) and *sdist1* (right).

CPU and 64 MB of main memory. As a baseline, to compare the query against $1,000$ documents, the optimal algorithms required 463.7 seconds for the 2-D case (*dist2*) and 964.0 seconds for the 1-D case (*dist1*). This extrapolates to 129 or 268 hours to search a hypothetical database of $1,000,000$ documents.

Table 3 below shows the speed-ups for the *hdist2* and *hdist1* heuristics. The threshold is a fraction of the maximum possible edit distance for the comparison in question. "Cells Computed" measures the percentage of the original computation that is performed by the heuristic. Note that the speed-up is not quite perfect. For example, for $\tau = 0.10$, 4.3% of the cells are computed by *hdist2*, but the runtime is 4.5% of the original. The situation is somewhat worse for the 1-D heuristic, as 4.5% of the cells are computed, but the runtime is 7.0% of *dist1*. This is due to the overhead of maintaining the livelist, as opposed to the simple loops of the original algorithms. Even so, a significant improvement in performance is evident. The runtimes to search a database of $1,000,000$ documents range from 2.2 to 103 hours.

	2-D Heuristic (*hdist2*)				1-D Heuristic (*hdist1*)			
Threshold	Cells Computed	Time	Speedup	Dupes Found	Cells Computed	Time	Speedup	Dupes Found
0.05	1.5%	7.8 s	×59.4	4/7	1.2%	18.9 s	×51.0	4/7
0.10	4.3%	21.0 s	×22.1	5/7	4.5%	67.3 s	×14.3	4/7
0.15	8.7%	42.2 s	×11.0	5/7	10.1%	147.7 s	×6.5	5/7
0.20	14.4%	70.0 s	×6.6	6/7	17.5%	254.8 s	×3.8	6/7
0.25	21.0%	101.8 s	×4.6	7/7	25.2%	370.2 s	×2.6	7/7

Table 3: Speed-ups for the heuristics for searching 1,000 documents.

The speed-ups for the *lbnddist2* pre-filter followed by the *hdist2* heuristic are given in Table 4. When the threshold is relatively tight only true duplicates pass the pre-filter, greatly accelerating the computation. Even when it is fairly loose, however, there is still a very large speed-up. The time to search a database of $1,000,000$ documents ranges between 53 and 105 minutes.

	Pre-Filter (*lbnddist2*) + 2-D Heuristic (*hdist2*)					
	Passed	Cells		Speedup		Dupes
Threshold	Pre-Filter	Computed	Time	Incremental	Aggregate	Found
0.05	4/1,000	0.03%	3.2 s	×2.4	×144.9	4/7
0.10	5/1,000	0.05%	3.4 s	×6.2	×136.4	5/7
0.15	13/1,000	0.09%	3.6 s	×11.7	×128.8	5/7
0.20	73/1,000	0.33%	4.5 s	×15.6	×103.0	6/7
0.25	130/1,000	0.75%	6.3 s	×16.2	×73.6	7/7

Table 4: Speed-ups for the two stage heuristic for searching 1,000 documents.

While impressive in this example, the performance of the pre-filter depends heavily on the distribution of line lengths in the database. Whereas *hdist1* and *hdist2* are more general techniques, *lbnddist2* is quite specific. It will not work as well in the case of documents with uniform line lengths, or when the cost functions are not as accommodating. If, for example, a low penalty is charged for certain common OCR errors, say space deletions and insertions, the bound, which is computed based on c_{mindel} and c_{minins} (Equation 14), becomes loose and the filter is much more porous.

7 Related Work

A number of researchers have begun to examine the problem of detecting duplicates in the context of document image databases [3, 11, 12, 13, 22, 24, 30]. For the most part, past work on the subject has concentrated on identifying which features to extract (the first step mentioned in Section 1) and not on the different ways they might be compared (the second step). The latter is typically handled using one or another of the techniques from the literature.

Broadly speaking, these approaches can be classified depending on whether they operate on low-level image features [11, 12, 22, 24] or on the output of a symbolic recognition process such as OCR [3, 13, 30]. The former are more general in the sense they can be applied to non-textual input (*e.g.*, drawings, photographs), but more limiting in that they can only be used to find full-layout duplicates.

Spitz, for example, employs character shape codes as features and compares them using the standard string matching algorithm (*i.e.*, Equation 1) [30]. In the taxonomy presented in Section 2, this corresponds to the full-content problem. Doermann, et al., also use shape codes, but extract n-grams for a specific text line to index into a table of document pointers [3]. Since this signature is computed from a single line, it does not explicitly measure the similarity of complete pages. The intention, though, is that this is a method for addressing the full-layout problem. Hull, et al., describe three techniques: one based on decomposing the page into a grid and counting connected components within each cell, another using word lengths as a hash key, and one comparing image features (pass codes arising from fax compression) under a Hausdorff distance measure [12]. More details on the last method appear in [11]. The first and third of these fall in the full-layout category,

while the second can be classified as searching for full-content duplicates. In a recent paper, Lee and Hull describe a method for performing duplicate detection on symbolically compressed images by solving the text deciphering problem through the use of Hidden Markov Models [13]. They then apply n-gram indexing with term weighting to detect duplicates, addressing the full-content problem.

Elsewhere, Taghva, et al., observed that traditional vector-space techniques from the field of information retrieval (IR) are for the most part unaffected by OCR errors when the input is relatively clean [32]. Also seemingly related is the general copy detection problem. Shivakumar and Garcia-Molina have developed efficient methods for searching large on-line databases for signs of copyright infringement [27]. A later paper of theirs considers the task of identifying near-replicas on the World Wide Web (WWW) to improve the performance of Web crawlers, archivers, and search engines [28]. All of these approaches are text-based, employing character or word n-grams or longer syntactic entities (sentences, paragraphs, etc.), and must allow for the fact that two documents need not be identical for the results of their comparison to qualify as "interesting." There are, however, significant differences between a typical IR query and a complete document, and between the kinds of errors that arise during OCR and the steps taken to conceal an attempt at plagiarism. A recent paper studied these issues from the standpoint of duplicate detection [18].

Lastly, techniques developed for searching large filesystems for similar files might be considered relevant. Manber presents such an algorithm based on computing checksums in predetermined "windows" [20]. Again, since file editing operations and OCR errors appear to be fundamentally different processes, it is not clear how well this kind of approach would work for the problem at hand.

8 Conclusions and Future Research

This paper has examined a number of issues related to the detection of duplicates in document image databases. Four distinct models for formalizing the problem were presented, along with algorithms for determining the optimal solution in each case. Experimental results demonstrate that the models match the real world, and the algorithms are robust with respect to the kinds of OCR errors that are likely to be encountered. Table 5 enumerates these classes one last time. A solid dot highlights the algorithm most suited to a particular problem, while a hollow dot indicates that the algorithm will find not only such duplicates but other types as well.

Duplicate		Algorithm			
Type	Examples	*dist2*	*dist1*	*sdist2*	*sdist1*
Full-layout	photocopies, faxes	●	○	○	○
Full-content	printed HTML		●		○
Partial-layout	redaction			●	○
Partial-content	copy-and-paste				●

Table 5: The optimal algorithms and where they apply.

Since some of the problems seem to subsume others, an obvious question is "Why bother with the less general ones?" The answer lies in increased precision for those situations where admitting a larger class of duplicates is undesirable (*e.g.*, when the targeted duplicates are known to be photocopies). Special cases also make it possible to develop more efficient algorithms.

Several heuristics were described for speeding up the full-duplicate computation. These techniques fall into a variety of categories, but all generally involve deriving an approximation to the distance measure of interest. It was proven that the heuristics will never miss a duplicate that would have been returned by the slower, optimal algorithms *dist1* and *dist2*. Experimentally, the speed-ups seen are impressive.

There are numerous ways this work could be extended. For example, there exists yet another model for approximate string matching known as "word-spotting" that applies when one of the strings must be matched in its entirety and the other is allowed the flexibility of choosing its most similar substring [26]. This might arise when a paragraph is copied out of one document and used to query the database for other pages that contain it. Again, there is a dynamic programming algorithm along the lines of Equations 2 and 4 that solves the problem. Although the *sdist* algorithms can also catch such duplicates, they do so at a potentially lower precision.

It may be advantageous to consider adding more levels to the symbol/line hierarchy. This could include text blocks as a collection of lines, columns as a collection of text blocks, and pages as a collection of columns. These would add new dimensions to the optimization problem, but the techniques already discussed may be generalizable. The most serious issue appears to be the requirement the system follow a unidirectional editing process at each level. Allowing arbitrary block motion overcomes this, however, and is addressed in another paper [19].

As noted earlier, the string algorithms are not limited to comparing ASCII characters. Examining alternate symbolic representations that are less expensive to compute than full-scale OCR, character shape codes for example [30], could prove to be productive.

Finally, there are a variety of questions concerning further speed-up of the computations. The livelist heuristic is reminiscent of a technique known as "branch-and-bound," although the order in which the search is performed is more regular making the data structures simpler. A true branch-and-bound implementation might potentially be faster than *hdist* if the overhead were not too severe. Since the file I/O alone for $1,000$ documents totals 2.6 seconds, however, it is not possible to improve the speed much beyond that shown in Table 4. Database indexing techniques consistent with the edit distance metric (for which performance guarantees could be proven) would make an interesting topic for future research. Likewise, the existence of any kind of heuristic with guaranteed performance for the partial-duplicate problems is an open question.

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