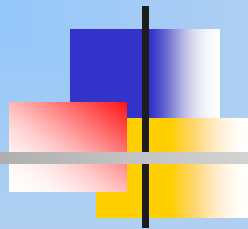
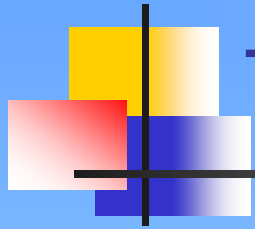


CSE302: Compiler Design



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P.C. Rossin College of Engineering & Applied Science
Lehigh University

January 18, 2007



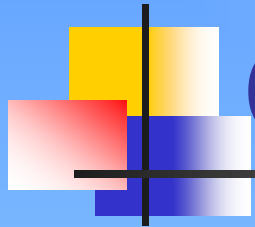
Today's Outline

- Recap
- A simple syntax-directed translator (Chapter 2)
 - Introduction (Section 2.1)
 - Syntax definition (Section 2.2)
 - Parsing (Section 2.4)
- Summary and homework



Six Compilation Phases

- Lexical analysis
- Syntax analysis
- Semantic analysis
- Intermediate code generation
- Code optimization
- Code generation



Outline

- Recap
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Contents in Chapter 2

- Illustrate some compiler techniques via developing a simple language translator coded in Java (Appendix A)
 - Source language
 - Target language: three-address code
- The front-end of a compiler



Six Compilation Phases

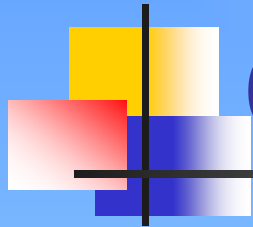
- Lexical analysis
- Syntax analysis
- Semantic analysis
- Intermediate code generation
- Code optimization
- Code generation

A Simplified Model of A Compiler Front End

- do $i=i+1$; while ($a[i]>v$);



- 1: $i = i + 1$
 $t1 = a[i]$
 if $t1 > v$ goto 1



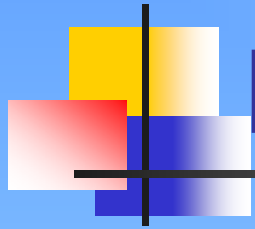
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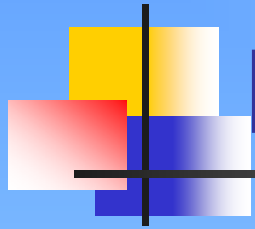
A Formal Method of Describing Syntax

- Backus-Naur Form (1959)
 - For Algol 58 (John Backus, the Peter Naur)
 - **BNF** is equivalent to **context-free grammars**
 - Context-free grammars were developed by Noam Chomsky in mid-1950s to define a class of languages called context-free languages
 - A BNF grammar defines a language
 - Recognizer vs. generators
 - A BNF grammar or description is a production-**rule** collection



BNF Rules

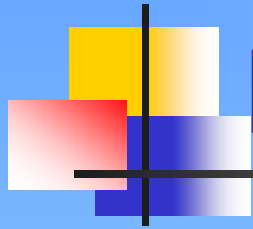
- A BNF rule defines an abstraction for syntactic structure
`<while_stmt> → while (<logic_expr>) <stmt>`
- Abstractions are used to represent classes of syntactic structures: they act like syntactic variables (also called **nonterminal symbols**)
- Terminal symbols: lexemes and tokens



LHS & RHS of BNF Rules

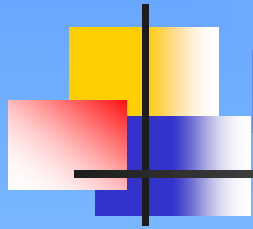
- A rule has a **left-hand side** (LHS) and a **right-hand side** (RHS), and consists of terminal and/or nonterminal symbols
- An abstraction (or nonterminal symbol) can have more than one RHS

```
<stmt> → <single_stmt>  
        | begin <stmt_list> end
```



BNF Functionality

- Describe grammars and derivations
 - Describe lists of similar constructs
 - Parse trees
- Powerful enough to avoid grammar ambiguity
 - Operator precedence and associativity



Describing Lists

BNF Functionality

- Describing Lists
- Grammar & Derivation
- Parse Trees
- Avoiding Ambiguity

- Syntactic lists are described using recursion

$$\langle \text{ident_list} \rangle \rightarrow \text{ident}$$
$$| \text{ident}, \langle \text{ident_list} \rangle$$

- A rule is **recursive** if its LHS appears in its RHS



A BNF Grammar

BNF Functionality

- Describing Lists
- Grammar & Derivation
- Parse Trees
- Avoiding Ambiguity

- A BNF grammar defines a language
- Sentences of a language are generated through applications of rules, beginning with a start symbol
- A grammar for a small language

$\langle \text{program} \rangle \rightarrow \langle \text{stmts} \rangle$

$\langle \text{stmts} \rangle \rightarrow \langle \text{stmt} \rangle \mid \langle \text{stmt} \rangle ; \langle \text{stmts} \rangle$

$\langle \text{stmt} \rangle \rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$

$\langle \text{var} \rangle \rightarrow \mathbf{a} \mid \mathbf{b} \mid \mathbf{c} \mid \mathbf{d}$

$\langle \text{expr} \rangle \rightarrow \langle \text{term} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle - \langle \text{term} \rangle$

$\langle \text{term} \rangle \rightarrow \langle \text{var} \rangle \mid \mathbf{const}$



Derivation

BNF Functionality

- Describing Lists
- Grammar & Derivation
- Parse Trees
- Avoiding Ambiguity

- A sentence generation is called a **derivation**
- An example derivation:

$\langle \text{program} \rangle \Rightarrow \langle \text{stmts} \rangle$

$\Rightarrow \langle \text{stmt} \rangle$

$\Rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$

$\Rightarrow \mathbf{a} = \langle \text{expr} \rangle$

$\Rightarrow \mathbf{a} = \langle \text{term} \rangle + \langle \text{term} \rangle$

$\Rightarrow \mathbf{a} = \langle \text{var} \rangle + \langle \text{term} \rangle$

$\Rightarrow \mathbf{a} = \mathbf{b} + \langle \text{term} \rangle$

$\Rightarrow \mathbf{a} = \mathbf{b} + \mathbf{const}$

$\langle \text{program} \rangle \rightarrow \langle \text{stmts} \rangle$

$\langle \text{stmts} \rangle \rightarrow \langle \text{stmt} \rangle \mid \langle \text{stmt} \rangle ; \langle \text{stmts} \rangle$

$\langle \text{stmt} \rangle \rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$

$\langle \text{var} \rangle \rightarrow \mathbf{a} \mid \mathbf{b} \mid \mathbf{c} \mid \mathbf{d}$

$\langle \text{expr} \rangle \rightarrow \langle \text{term} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle - \langle \text{term} \rangle$

$\langle \text{term} \rangle \rightarrow \langle \text{var} \rangle \mid \mathbf{const}$



Terms in Derivation

BNF Functionality

- Describing Lists
- Grammar & Derivation
- Parse Trees
- Avoiding Ambiguity

- Every string of symbols in the derivation is a **sentential form**
- A **sentence** is a sentential form that has only terminal symbols
- A **leftmost derivation** is one in which the leftmost nonterminal in each sentential form is the one that is expanded
- A derivation may be neither leftmost nor rightmost

```
<program> => <stmts>
=> <stmt>
=> <var> = <expr>
=> a = <expr>
=> a = <term> + <term>
=> a = <var> + <term>
=> a = b + <term>
=> a = b + const
```



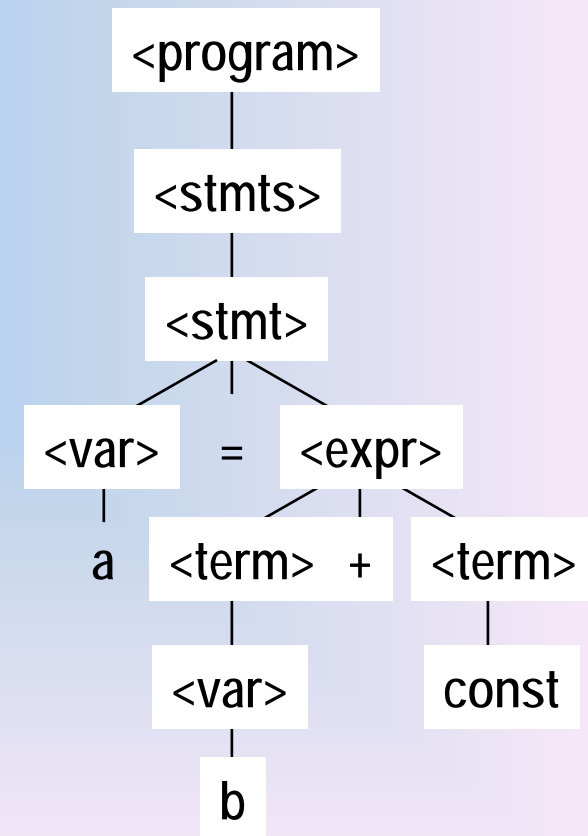
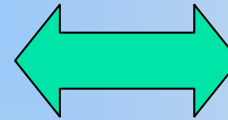

Parse Tree

BNF Functionality

- Describing Lists
- Grammar & Derivation
- Parse Trees
- Avoiding Ambiguity

- A hierarchical representation of a derivation

$\langle \text{program} \rangle \Rightarrow \langle \text{stmts} \rangle$
 $\Rightarrow \langle \text{stmt} \rangle$
 $\Rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$
 $\Rightarrow \mathbf{a} = \langle \text{expr} \rangle$
 $\Rightarrow \mathbf{a} = \langle \text{term} \rangle + \langle \text{term} \rangle$
 $\Rightarrow \mathbf{a} = \langle \text{var} \rangle + \langle \text{term} \rangle$
 $\Rightarrow \mathbf{a} = \mathbf{b} + \langle \text{term} \rangle$
 $\Rightarrow \mathbf{a} = \mathbf{b} + \mathbf{const}$



Lists, Grammar, and Parse Trees

BNF Functionality

- Describing Lists
- Grammar & Derivation
- Parse Trees
- Avoiding Ambiguity

$\langle \text{program} \rangle \rightarrow \langle \text{stmts} \rangle$

$\langle \text{stmts} \rangle \rightarrow \langle \text{stmt} \rangle \mid \langle \text{stmt} \rangle ; \langle \text{stmts} \rangle$

$\langle \text{stmt} \rangle \rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$

$\langle \text{var} \rangle \rightarrow a \mid b \mid c \mid d$

$\langle \text{expr} \rangle \rightarrow \langle \text{term} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle - \langle \text{term} \rangle$

$\langle \text{term} \rangle \rightarrow \langle \text{var} \rangle \mid \text{const}$

$\langle \text{program} \rangle$

$\Rightarrow \langle \text{stmts} \rangle$

$\Rightarrow \langle \text{stmt} \rangle$

$\Rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$

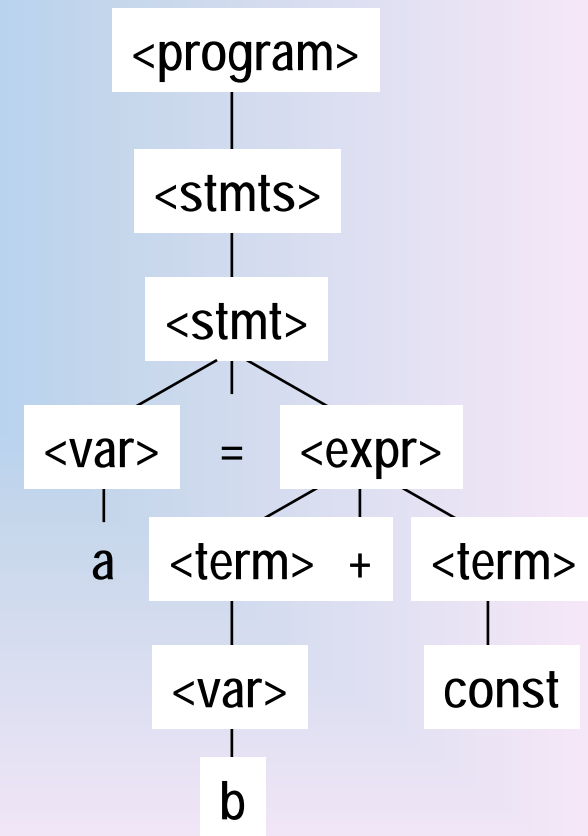
$\Rightarrow a = \langle \text{expr} \rangle$

$\Rightarrow a = \langle \text{term} \rangle + \langle \text{term} \rangle$

$\Rightarrow a = \langle \text{var} \rangle + \langle \text{term} \rangle$

$\Rightarrow a = b + \langle \text{term} \rangle$

$\Rightarrow a = b + \text{const}$





Avoiding Ambiguity

BNF Functionality

- Describing Lists
- Grammar & Derivation
- Parse Trees
- **Avoiding Ambiguity**

- A grammar is **ambiguous** iff it generates a sentential form that has two or more distinct parse trees
 - Operator precedence ambiguity
 - Operator associativity ambiguity
 - ...

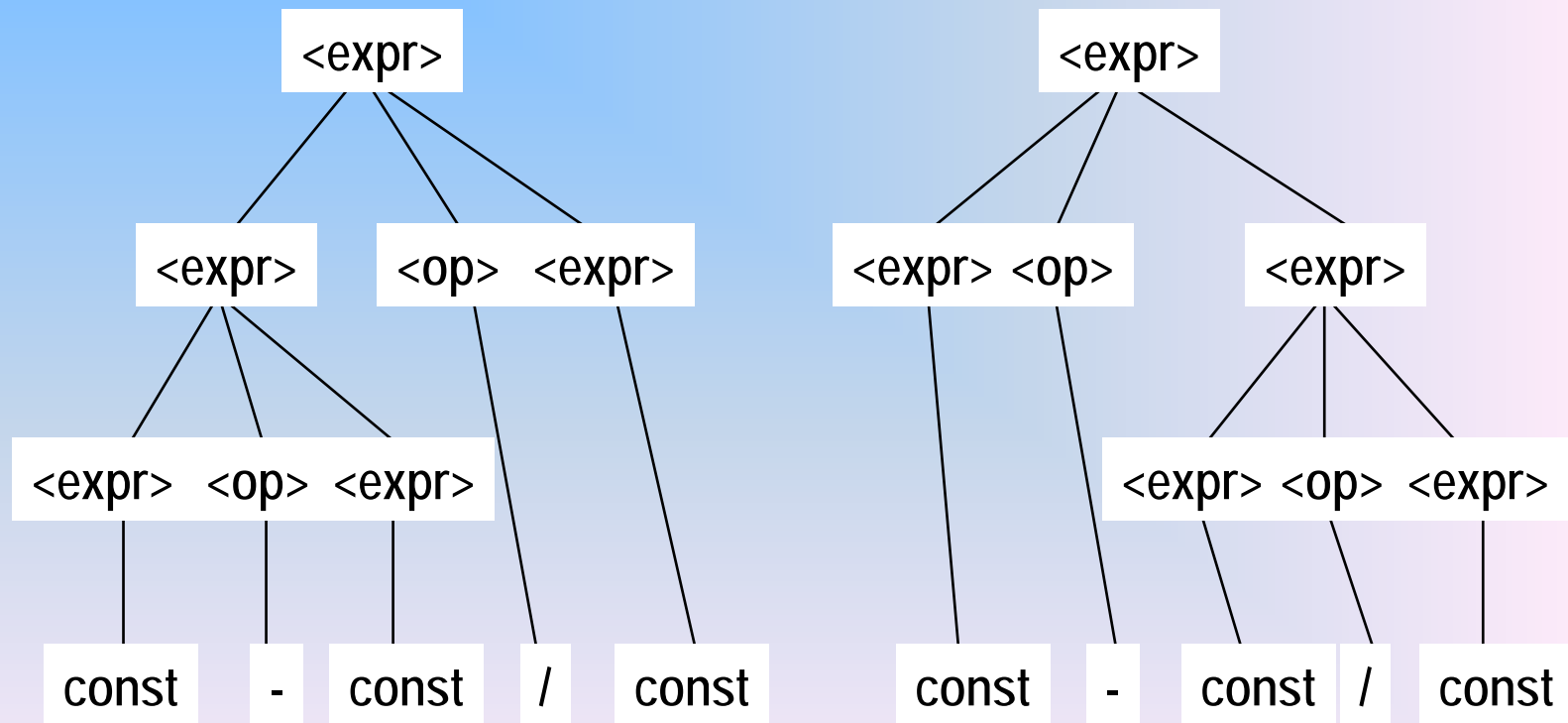
An Ambiguous Expression Grammar

BNF Functionality

- Describing Lists
- Grammar & Derivation
- Parse Trees
- **Avoiding Ambiguity**

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle \langle \text{op} \rangle \langle \text{expr} \rangle \mid \text{const}$

$\langle \text{op} \rangle \rightarrow / \mid -$





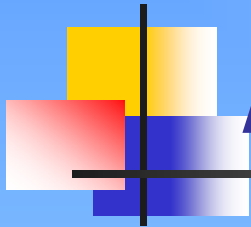
An Unambiguous Expression Grammar

BNF Functionality

- Describing Lists
- Grammar & Derivation
- Parse Trees
- **Avoiding Ambiguity**

- If we use an additional nonterminal to indicate precedence levels of the operators, we will not have such ambiguity

$$\begin{aligned} \langle \text{expr} \rangle &\rightarrow \langle \text{expr} \rangle - \langle \text{term} \rangle \mid \langle \text{term} \rangle \\ \langle \text{term} \rangle &\rightarrow \langle \text{term} \rangle / \mathbf{const} \mid \mathbf{const} \end{aligned}$$



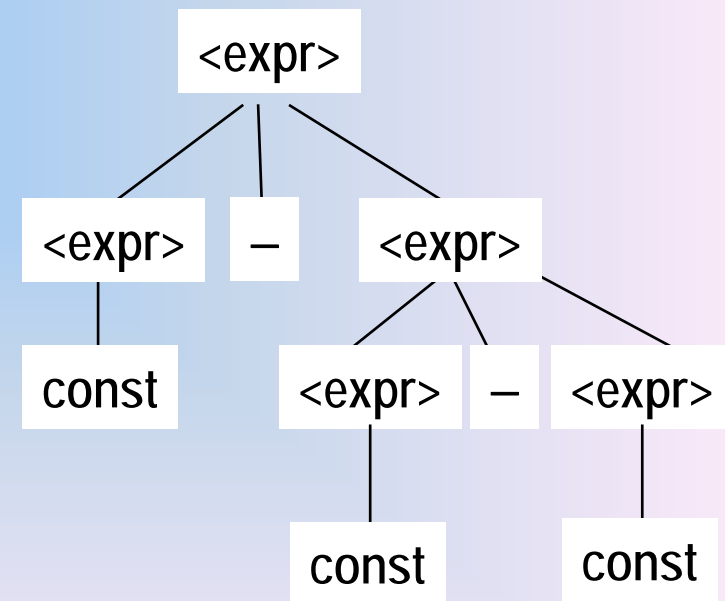
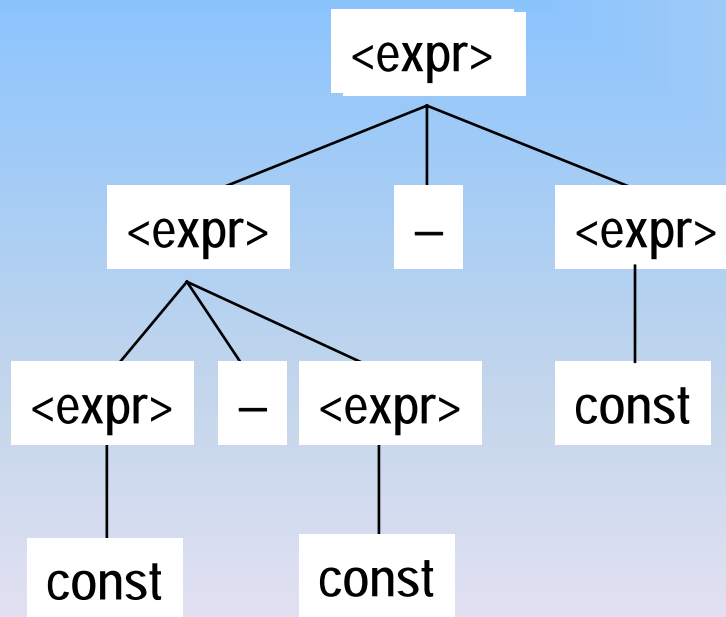
Another Ambiguity

BNF Functionality

- Describing Lists
- Grammar & Derivation
- Parse Trees
- **Avoiding Ambiguity**

- Operator associativity ambiguity

<expr> -> <expr> - <expr> | const (ambiguous)



Avoid Ambiguity

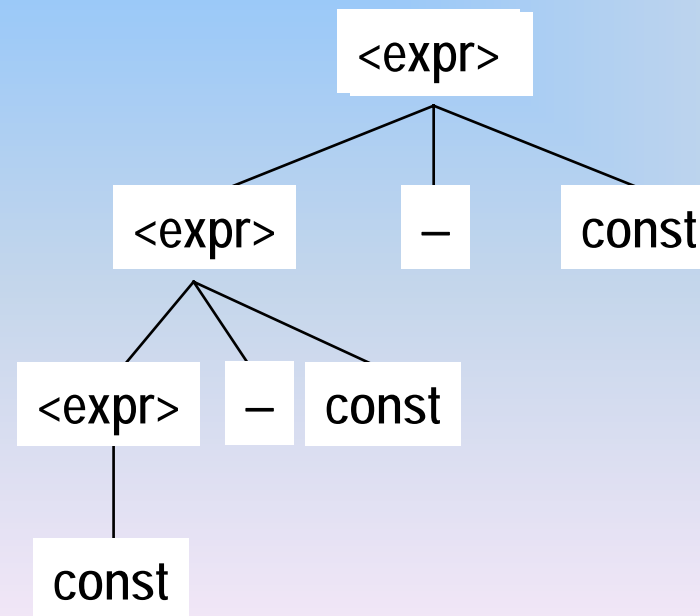
BNF Functionality

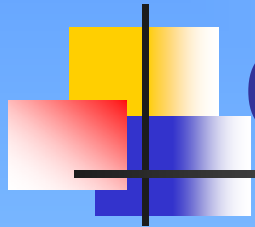
- Describing Lists
- Grammar & Derivation
- Parse Trees
- **Avoiding Ambiguity**

- Operator associativity can also be indicated by a BNF description

<expr> -> <expr> - <expr> | const (ambiguous)

<expr> -> <expr> - const | const (unambiguous)





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 - Parsing (Section 2.4.1-2.4.4)
- Summary and homework



Parsing

- Parsing is the process of determining how a string of terminals can be generated by a grammar
 - Parse tree generation
 - Parsers make a single left-to-right scan over the input tokens, look ahead of one terminal at a time, and construct the parse tree.
- Top-down parsing vs. bottom-up parsing



Predictive Parsing (1)

- A Recursive-Descent Parser
 - Directly following the BNF grammar
 - $\langle \text{expr} \rangle \rightarrow \langle \text{term} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle - \langle \text{term} \rangle \mid \langle \text{term} \rangle$
 - $\langle \text{term} \rangle \rightarrow 0 \mid 1 \mid 2 \mid \dots \mid 9$

- Pseudo code

```
void expr() {  
    term();  
    if( token==plus_op  
        or token==minus_op) {  
        match(token);  
        term();  
    }  
    else error();  
}
```

```
void term() {  
    match(int_literal);  
}
```

```
void match(expectedToken) {  
    if(token==expectedToken)  
        getNextToken();  
    else error();  
}
```

- Demo

- A homework question



Predictive Parsing (2)

- A BNF grammar
 - $\text{stmt} \rightarrow \mathbf{expr}; \mid \mathbf{for}(\text{optexpr}; \text{optexpr}; \text{optexpr}) \text{stmt} \mid \mathbf{other}$
 - $\text{optexpr} \rightarrow \varepsilon \mid \mathbf{expr}$
- Pseudo code

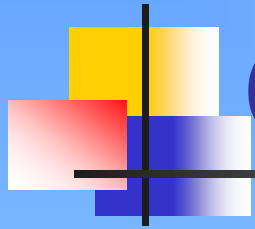
```
void stmt() {
    switch ( lookahead ) {
        case expr:
            match(expr); match(';'); break;
        case for:
            match(for); match('('); optexpr(); match(';'); optexpr(); match(';');
            optexpr(); match(')'); stmt(); break;
        case other:
            match(other); break;
        default: report("Syntax error");
    }
}

void optexpr() { if ( lookahead == expr ) match(expr); }
void match(terminal t) {
    if ( lookahead == t ) lookahead = nextToken; else report("Syntax error"); }
```



Predictive Parsing (3)

- A BNF grammar
 - $\text{stmt} \rightarrow \mathbf{expr}; \mid \mathbf{if}(\mathbf{expr}) \text{ stmt} \mid \mathbf{for}(\text{optexpr}; \text{optexpr}; \text{optexpr}) \text{ stmt} \mid \mathbf{other}$
 - $\text{optexpr} \rightarrow \varepsilon \mid \mathbf{expr}$
- A statement
 - $\text{for} (; \text{expr} ; \text{expr}) \text{ other}$



Outline

- Recap
- A simple syntax-directed translator (Chapter 2)
- **Summary and homework**



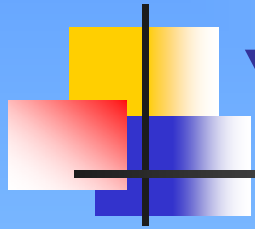
You should now be able to ...

- Evaluate whether a grammar is ambiguous;
- Use BNF to specify operator precedence;
- Write a simple recursive-descent parser.



Grammar Ambiguity

- A grammar is **ambiguous** iff it generates a sentential form that has two or more distinct parse trees
- Every derivation with an unambiguous grammar has a unique parse tree, although that tree can be represented by different derivations



You should now be able to ...

- Evaluate whether a grammar is ambiguous;
- Use BNF to specify operator precedence and associativity;
- Write a simple recursive-descent parser.



Operator Precedence by BNF

- Guidelines
 - Use terminal operator lexemes
 - Use additional nonterminals as operands

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle \langle \text{op} \rangle \langle \text{expr} \rangle \mid \text{const}$

$\langle \text{op} \rangle \rightarrow / \mid -$

An ambiguous grammar

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle - \langle \text{term} \rangle \mid \langle \text{term} \rangle$

$\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle / \text{const} \mid \text{const}$

An unambiguous grammar



Operator Associativity by BNF

- Operator associativity can also be indicated by a BNF description

<expr> -> <expr> + <expr> | const (ambiguous)

<expr> -> <expr> + const | const (unambiguous)

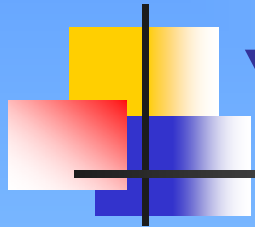
- Guidelines

- A rule's LHS appears at the beginning of its RHS, which is a **left-recursive** rule. Then it indicates left associativity.
- Right associativity (**LHS is the operand at the right-hand side, not at the left**)

- Exponentiation operator

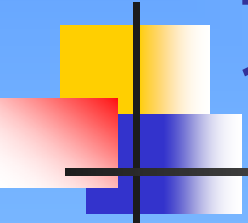
<expr> -> <base> ** <expr> | <base>

<base> -> id | const



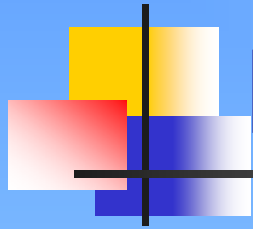
You should now be able to ...

- Evaluate whether a grammar is ambiguous;
- Use BNF to specify operator precedence and associativity;
- Write a simple recursive-descent parser.



Homework (Due on 01/22 at 11:55 PM)

- 1.1. (10 points) Just as shown in Figure 1.7 in the textbook (page 7), detail the six steps of compilation for the statement: $A=B*5+C/3$ where A, B, C are variables of floating-point type.
- 1.2. (10 points) Consider the context-free grammar:
$$S \rightarrow + S S \mid - S S \mid a$$
 - a) Show how the string $+a-aa$ can be generated by this grammar.
 - b) Construct a parse tree for this same string.
- 1.3. (10 points) Implement an executable and correct recursive-descent parser based on the pseudo code for the BNF grammar illustrated in this lecture:
 - $\langle \text{expr} \rangle \rightarrow \langle \text{term} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle - \langle \text{term} \rangle \mid \langle \text{term} \rangle$
 - $\langle \text{term} \rangle \rightarrow 0 \mid 1 \mid 2 \mid \dots \mid 9$



Reading Assignment

- Chapter 18 in The Java Language Specification, Third Edition
 - The Grammar of the Java Programming Language
 - <http://java.sun.com/docs/books/jls/>